Multiple-choice Questions:

1. A particle is moving in a circular path of radius r. The displacement after half a circle would be:

(a) Zero

(b) π r

(c) 2 r

(d) 2π r

Soln:

The answer is (c) 2 r.

Explanation: After half revolution

Distance travelled = X circumference= πr

Path length Displacement = Final position- Initial Position

It comes out to be the diameter of the circle = 2 r.

2. A body is thrown vertically upward with velocity u, the greatest height h to which it will rise is,

(a) u/g

(b) $u^2/2g$

(c) u^2/g

(d) u/2g

Answer: (b) $u^2/2g$.

Explanation:

$V^2= u^2+2$ as

here v = 0

a = -g

s = H

$0 = u^2 - 2gH$

$H = u^2/2g$

Solution 2:

(b) At highest point, v = 0
Using $v^2 - u^2 = 2as$, we get
$0 - u^2 = 2(-g)h$ (∵ a=-g and s=h)
or $h=u^2/2g$

3. The numerical ratio of displacement to the distance for a moving object is

(a) always less than 1

(b) always equal to 1

(c) always more than 1

(d) equal or less than 1

Answer: (d) equal or less than 1

Explanation:

- The shortest distance between the initial and the endpoint is called displacement. Distance is the total path length.
- Displacement is vector, and it may be positive or negative, whereas Distance is scalar, and it can never be negative.
- The distance can be equal to or greater than displacement, which means the ratio of displacement to distance is always equal to or less than 1.

4. If the displacement of an object is proportional to square of time, then the object moves with

(a) uniform velocity

(b) uniform acceleration

(c) increasing acceleration

(d) decreasing acceleration

Answer: (b) uniform acceleration

Explanation: Velocity is measured in distance/second, and acceleration is measured in distance second^2. Hence uniform acceleration is the right answer.

5. From the given v – t graph (Fig. 8.1), it can be inferred that the object is

(a) in uniform motion

(b) at rest

(c) in non-uniform motion

(d) moving with uniform acceleration

Answer: (a) in uniform motion

Explanation: From the above-given graph, it is clear that the velocity of the object remains constant throughout hence the object is in uniform motion.

6. Suppose a boy is enjoying a ride on a merry-go-round which is moving at a constant speed of 10 m/s. It implies that the boy is

(a) at rest

(b) moving with no acceleration

(c) in accelerated motion

(d) moving with uniform velocity

Answer: (c) in accelerated motion

Explanation: The boy is moving in a circular motion, and circular motion is an accelerated motion; hence C) is the right answer.

7. Area under a v – t graph represents a physical quantity which has the unit

(a) m^2

(b) m

(c) m^3

(d) $m\ s^{-1}$

Answer: (b) m

Explanation: The area given in the graph represents Displacement, and its unit is meter. Hence, the answer is (b) m.

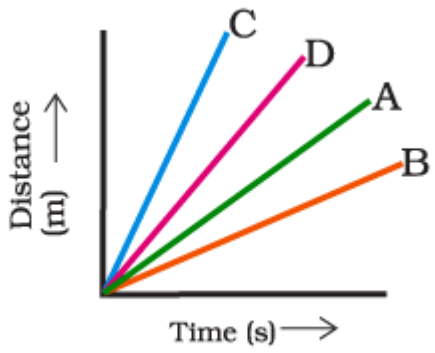
8. Four cars, A, B, C and D, are moving on a levelled road. Their distance versus time graphs are shown in Fig. 8.2. Choose the correct statement

(a) Car A is faster than car D.

(b) Car B is the slowest.

(c) Car D is faster than car C.

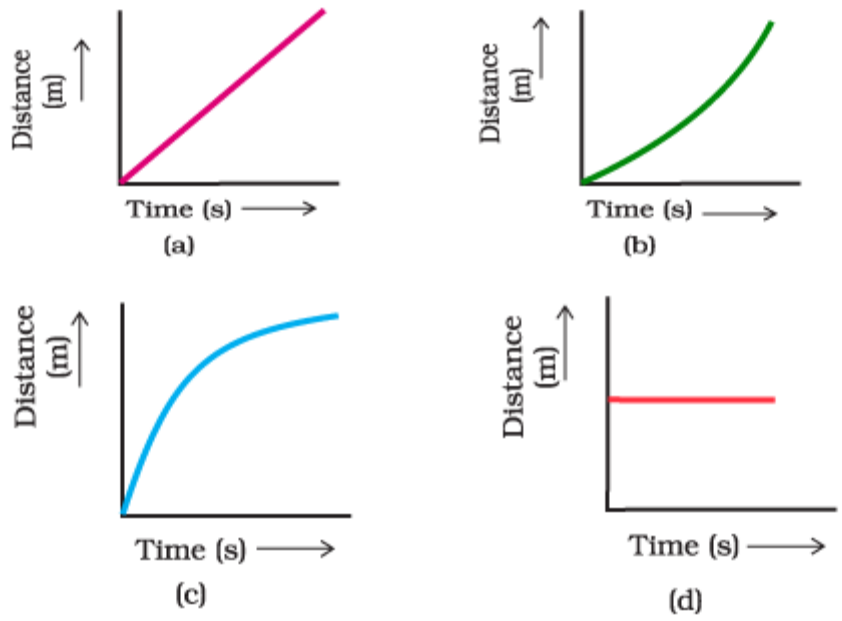
(d) Car C is the slowest.



Answer: (b) Car B is the slowest.

Explanation: The graph shows that Car B covers less distance in a given time than A, C and D cars hence it is the slowest.

9. Which of the following figures (Fig. 8.3) represents the uniform motion of a moving object correctly?



Answer: (a)

Explanation: Distance in graph a) is uniformly increasing with time hence it represents uniform motion.

10. Slope of a velocity–time graph gives

(a) the distance

(b) the displacement

(c) the acceleration

(d) the speed

Answer: (c) the acceleration

11. In which of the following cases of motions the distance moved and the magnitude of displacement are equal?

(a) If the car is moving on a straight road

(b) If the car is moving in a circular path

(c) The pendulum is moving to and fro

(d) The earth is revolving around the Sun

Answer: (a) If the car is moving on a straight road

Explanation: In other cases given here, displacement can be less than distance; hence option (a) If the car is moving on a straight road, is the right answer.

Short Answer Questions:

12. The displacement of a moving object in a given interval of time is zero. Would the distance travelled by the object also be zero? Justify your answer.

Answer: Displacement zero does not mean zero distance. The distance can be zero when moving an object back to the place it started. Displacement is either equal to or less than distance, but the distance is always greater than one, and it cannot be a negative value.

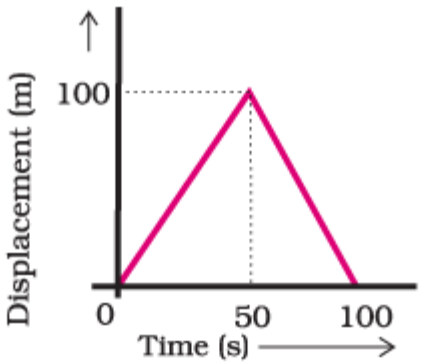
13. How will the equations of motion for an object moving with a uniform velocity change?

Answer: If the object is moving with a uniform velocity, then v = μ and a = 0. In this scenario equation for distance is given below.

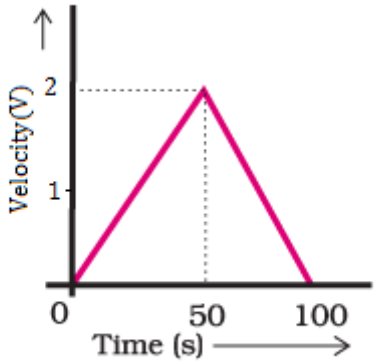
S= ut and $V^2 - \mu^2 = 0$

$\therefore$ Equation of motions $v = u + at$, $s = ut + \frac{1}{2} at^2$
and $v^2 - u^2 = 2as$ change to $v = u$, $s = ut$ and $v = u$

14. A girl walks along a straight path to drop a letter in the letterbox and comes back to her initial position. Her displacement–time graph is shown in Fig.8.4. Plot a velocity-time graph for the same.



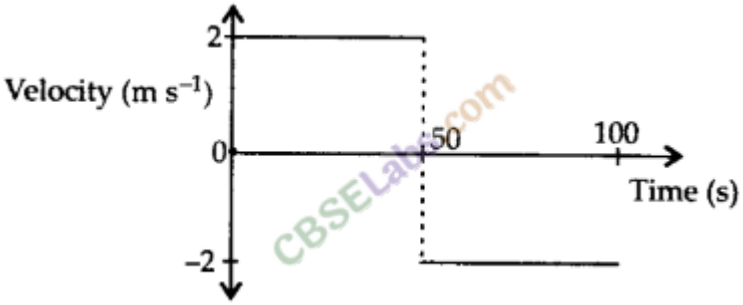
Answer:



From displacement – time graph,

$$\text{velocity} = \frac{\text{displacement}}{\text{time}} = \frac{100\ \text{m}}{50\ \text{s}} = 2\ \text{m s}^{-1}$$

Symmetry of graph shows that the girl comes back to her initial position with same velocity (2 ms^{-1}) but in opposite direction. So, the velocity-time graph will look like



15. A car starts from rest and moves along the x-axis with a constant acceleration of 5 m/s^2 for 8 seconds. If it then continues with constant velocity, what distance will the car cover in 12 seconds since it started from the rest?

Soln:

Car Starts from rest hence Initial velocity u=o acceleration a=5 m/s^2 and time t=8s

v = u+at

v = 0+5×8

v = 40ms^{-1}

From second equation

$s = ut + \frac{1}{2} at^2$

$s = 0 \times 8 + \frac{1}{2} \times 5 \times (8)^2$

$s = \frac{1}{2} \times 5 \times (8)^2$

$s = \frac{1}{2} \times 5 \times 64$

s = 5×32 =160 is the distance covered in 8 seconds.

Therefore, the total distance covered in 12 seconds is 160+160 = 320 m

Solution 2:

For constant acceleration of car,
$u = 0, a = 5 \text{ m s}^{-2}, t = 8 \text{ s}$
Using $s = ut + \frac{1}{2} at^2$, we get
$s_1 = 0 + \frac{1}{2} \times 5 \times 8^2 = 160 \text{ m}.$
For constant velocity of car,
$v = u + at = 0 + 5 \times 8 = 40 \text{ m s}^{-1},$
$t = (12 - 8) \text{ s} = 4 \text{ s}, a = 0$
$\therefore s_2 = vt = 40 \times 4 = 160 \text{ m}.$
Therefore, total distance covered in 12 s
$= s_1 + s_2 = 160 + 160 = 320 \text{ m}.$

16. A motorcyclist drives from A to B with a uniform speed of 30 km/h and returns back with a speed of 20 km h^{-1}. Find its average speed.

Answer:

Let the distance from A to B is D kms.

Distance for the entire journey is 2D kms.

The time taken to go from A to B is D/30 hr, and that of B to A is D/20 hr. So, the total time taken T is

T = (D/30) + (D/20). By solving, we will get,

T = D/12 hrs.

Average speed = Total distance/Total time.

Av.speed = 2D ÷ D/12

=> 2D x 12/D = 24 km/h.

Hence Average speed of the motorcycle is 24 km/h.

Solution 2:

Let the distance between A and B be S km.

Time taken in going from A to $B = \frac{S}{30} h$.

Time taken in going from B to $A = \frac{S}{20} h$.

Average speed of motorcyclist

$$= \frac{\text{total distance covered}}{\text{total time taken}}$$

$$= \frac{S \text{ km} + S \text{ km}}{\frac{S}{30} h + \frac{S}{20} h} = \frac{2}{\frac{1}{30} + \frac{1}{20}} \text{ km h}^{-1}$$

$$= \frac{2}{\frac{1}{12}} \text{ km h}^{-1} = 24 \text{ km h}^{-1}.$$

17. The velocity-time graph (Fig. 8.5) shows the motion of a cyclist. Find (i) its acceleration, (ii) its velocity, and (iii) the distance covered by the cyclist in 15 seconds

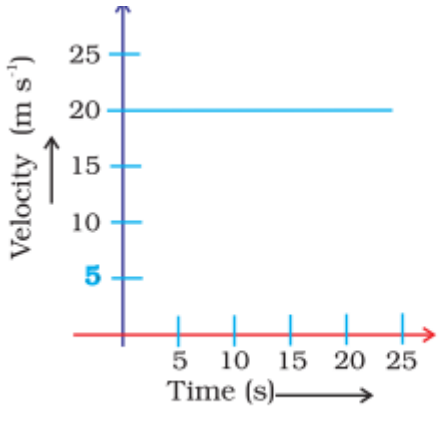


Fig. 8.5

Answer:

(i) As velocity is constant, acceleration is 0 m/s^2

(ii) Here, the velocity is constant, hence v=20m/s

(iii) s = v x t

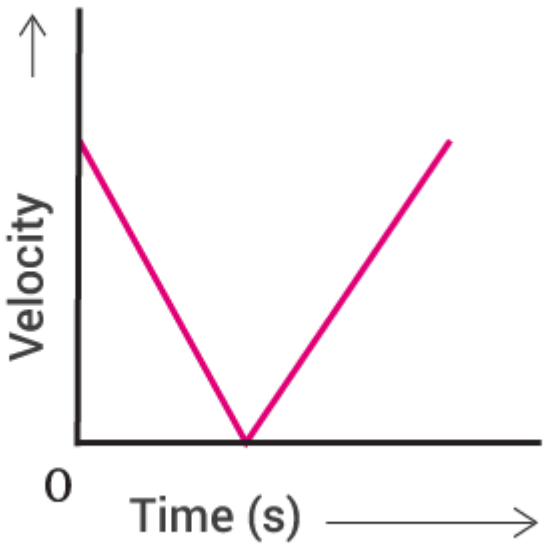
= 20 x 15

= 300 m

18. Draw a velocity versus time graph of a stone thrown vertically upwards and then coming downwards after attaining the maximum height.

Answer:

The velocity versus time graph of a stone thrown upwards vertically is as given below:



19. An object is dropped from rest at a height of 150 m, and simultaneously another object is dropped from rest at a height of 100 m. What is the difference in their heights after 2 s if both the objects drop with the same accelerations? How does the difference in heights vary with time?

Answer: When two objects fall with the same acceleration simultaneously, after 2 seconds, the difference in their heights will not change, and it remains 50 m.

$d_1 = h_1 - s_1$

$d_1 = 150 - \frac{1}{2}at^2 = 150 - \left(\frac{1}{2} \times 10 \times 4\right)$

$d_1 = 150 - 20 = 130$ m

Therefore the height of the first object after 2 seconds is 130 m.

In the same way, the height of the second object is

$d_2 = h_2 - s_2$

$d_2 = 100 - \frac{1}{2}at^2 = 100 - \left(\frac{1}{2} \times 10 \times 4\right)$

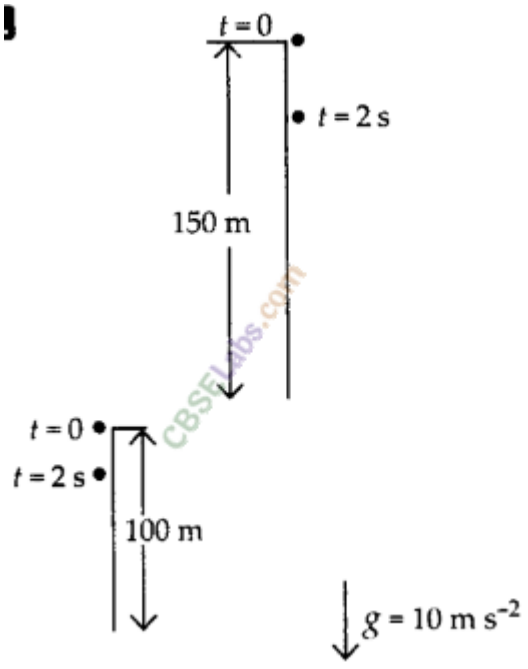
$d_1 = 100 - 20 = 80$ m

Therefore, the height of the second object after 2 seconds is 80 m.

So, the difference is the same, i.e. 50 m.

This concludes that the difference in the height of the two objects does not depend on time and will always be the same.

Solutions 2:



Initially, difference in heights of two objects
= 150 m – 100 m = 50 m
Distance travelled by first object in 2 s

$h = ut + \frac{1}{2} at^2 = 0 + \frac{1}{2} \times 10 \times 2 \times 2 = 20$ m

Distance travelled by the second object in 2 s,

$h' = ut + \frac{1}{2} at^2 = 0 + \frac{1}{2} \times 10 \times 2 \times 2 = 20$ m

Height of first object from ground at $t = 2$ s
= 150 m – 20 m = 130 m
Height of second object from ground at $t = 2$ s
= 100 m – 20 m = 80 m
∴ Difference in height after $t = 2$ s
= 130 m – 80 m = 50 m.

Difference in heights does not vary with time as long as both the objects are in motion. However, when second object reaches ground and first one is still in motion, then it decreases.

20. An object starting from rest travels 20 m in first 2 s and 160 m in next 4 s. What will be the velocity after 7 s from the start?

Answer:

Here Object starts from rest hence initial velocity u=0 t =2s and s=20 m

According to the second equation of motion $s= ut+at^2$

$S = 0 + \frac{1}{2} a \times 2^2$

$20 = 2+ \frac{1}{2} a \times 2^2 = 2a$

= 20/2

a = 10m/s

According to the first equation of motion velocity after 7 s from the start

V = u+at

V = 0+10×7

V = 70m/s

Solution 2:

For first 2 s motion of object,
u = 0, f = 2 s, s = 20 m.

Using $s = ut + \frac{1}{2}at^2$, we get $20 = 0 + \frac{1}{2}a \times 2^2$

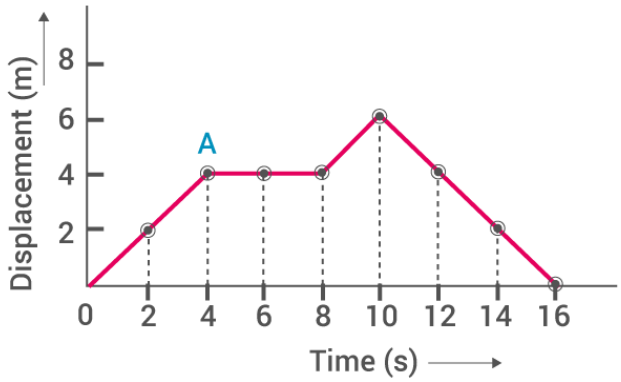
or $a = 10\ \text{m s}^{-2}$.
Velocity attained by object at the end of 2 s
$v = u + at = 0 + 10 \times 2 = 20\ \text{m s}^{-1}$.
For next 4 s, journey of object,
$t' = 4\ \text{s}, u' = 20\ \text{m s}^{-1}, s' = 160\ \text{m}$
$\therefore s' = u't' + \frac{1}{2}a't'^2$
$\Rightarrow 160 = 20 \times 4 + \frac{1}{2} \times a' \times 4^2$
or $8a' = 80$ or $a' = 10\ \text{m s}^{-2}$.
It implies that acceleration is uniform throughout the journey.
$\therefore$ velocity after 7 s from start, $v = u + at$
$= 0 + 10 \times 7 = 70\ \text{m s}^{-1}$.

21. Using the following data, draw time-displacement graph for a moving object:

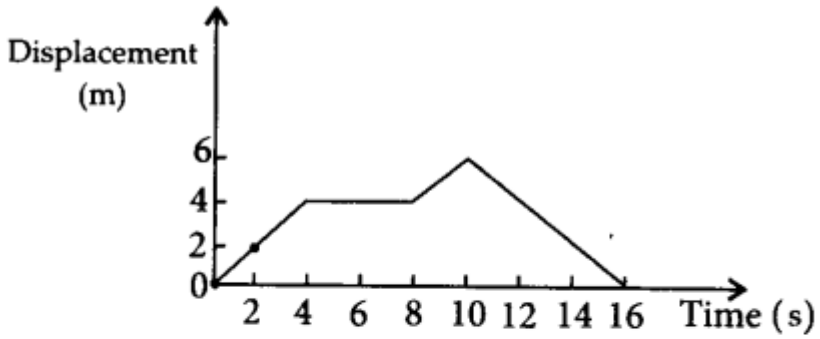
Time (s)	P	2	4	6	8	10	12	14	16
Displacement (m)	0	2	4	4	4	6	4	2	0

Use this graph to find the average velocity for the first 4 s, for the next 4 s and for the last 6 s.

Answer:



From the given data, displacement-time graph is shown as



$$\text{Average velocity} = \frac{\text{change in displacement}}{\text{time interval}}$$

$\therefore$ For first 4 s, $v_1 = \frac{4-0}{4} = 1 \text{ m s}^{-1}$

For next 4 s, $v_2 = \frac{4-4}{4} = 0 \text{ m s}^{-1}$

For last 6 s, $v_3 = \frac{0-6}{6} = -1 \text{ m s}^{-1}$

22. An electron moving with a velocity of 5 x 104 ms-1 enters into a uniform electric field and acquires a uniform acceleration of 104 m s~2 in the direction of its initial motion.
(i) Calculate the time in which the electron would acquire a velocity double of its initial velocity.
(ii) How much distance the electron would cover in this time?

Answer: Here initial velocity of electron ,

$u = 5 \times 10^4 \text{ m s}^{-1}$
acceleration, $a = 10^4 \text{ m s}^{-2}$
(i) $v = 2u = 2 \times 5 \times 10^4 \text{ m s}^{-1} = 10 \times 10^4 \text{ m s}$
using $v = u + at$, we get
$10 \times 10^4 = 5 \times 10^4 + 10^4 \times t$ or $t = 5$ s
(ii) Using $s = ut + \frac{1}{2}at^2$, we get

$s = 5 \times 10^4 \times 5 + \frac{1}{2} \times 10^4 \times 5^2$
$= 25 \times 10^4 + 12.5 \times 10^4 = 37.5 \times 10^4$ m.

23. Obtain a relation for the distance travelled by an object moving with a uniform acceleration in the interval between the 4th and 5th seconds.

Answer: a = dv/dt

Assume that air resistance is nil.

We can directly contain it by using Newton's equations of motion or from the below-mentioned method:

Thus, the area under the v-t curve and the x-axis where the slope of the curve is the instantaneous acceleration.

In this case, acceleration g is constant, and due to the free-fall condition, the initial velocity is zero. Therefore the v-t curve is a straight line with a slope equal to g equal to 9.81 m/s passing through the origin.

On dividing the total area under the curve into the interval of unit seconds, then we initially obtain a triangle followed by trapeziums of increasing height.

The ratio of the area of the first triangle to the second triangle to the third triangle is equal to the ratio of displacement in the first, second and third second. We get ratio equal to 1:3:5:7:9… and so on.

For the 4th & 5th second, it is 7:9.

Solution 2: Let the object be moving with initial velocity u m s^{-1} and uniform acceleration a ms^{-2} .

$\therefore$ The distance travelled by the moving object in t s is, $s = ut + \frac{1}{2}at^2$

Now, distance travelled in 4 s,

$s_4 = u \times 4 + \frac{1}{2}a \times 4^2 = 4u + 8a$

Distance travelled in 5 s,

$s_5 = u \times 5 + \frac{1}{2}a \times 5^2 = 5u + \frac{25}{2}a$

$\therefore$ Distance travelled in the interval between 4^{th} and 5^{th} second

$$= \left(5u + \frac{25}{2}a\right) - (4u + 8a) = \left(u + \frac{9}{2}a\right) \text{m}$$

24. Two stones are thrown vertically upwards simultaneously with their initial velocities u1 and u2, respectively. Prove that the heights reached by them would be in the ratio of $u1^2 : u2^2$

(Assume upward acceleration is –g and downward acceleration is +g).

Answer:

We know for upward motion, $v^2 = u^2 - 2gh$ or $h = \frac{u^2 - v^2}{2g}$

But at highest point $v = 0$

Therefore, $h = u^2/2g$

For first ball, $h_1 = u_1^2/2g$

and for second ball, $h_2 = u_2^2/2g$

Thus $\frac{h_1}{h_2} = \frac{u_1^2/2g}{u_2^2/2g} = \frac{u_1^2}{u_2^2}$ or $h_1 : h_2 = u_1^2 : u_2^2$

Solution 2: At the highest point, v=0
For the same thrown with velocity u_1

$0 - u^2_1 = 2(-g)h_1$ (Using, $v^2 - u^2 = 2as$)

or $h_1 = \frac{u_1^2}{2g}$

Similarly, for the stone thrown with velocity u_2,

$h_2 = \frac{u_2^2}{2g}$,

$\therefore$ The required ratio, $\frac{h_1}{h_2} = \frac{u_1^2}{2g} \times \frac{2g}{u_2^2} = \frac{u_1^2}{u_2^2}$.