



Exercise 1.1 Page: 5

Q1. Is zero a rational number? Can you write it in the form p/q where p and q are integers and $q \neq 0$?

Answer: We know that a number is said to be rational if it can be written in the form p/q , where p and q are integers and $q \neq 0$.

Taking the case of '0',

Zero can be written in the form $0/1, 0/2, 0/3 \dots$ as well as $, 0/1, 0/2, 0/3 \dots$

Since it satisfies the necessary condition, we can conclude that 0 can be written in the p/q form, where q can either be positive or negative number.

Hence, 0 is a rational number.

Q2. Find six rational numbers between 3 and 4.

Answer:

The rational numbers between 3 and 4.

$$\text{We have, } 3 = 3 \times \frac{(6+1)}{(6+1)} = \frac{21}{7} \text{ and } 4 = 4 \times \frac{(6+1)}{(6+1)} = \frac{28}{7}$$

We know that $21 < 22 < 23 < 24 < 25 < 26 < 27 < 28$

$$\Rightarrow \frac{21}{7} < \frac{22}{7} < \frac{23}{7} < \frac{24}{7} < \frac{25}{7} < \frac{26}{7} < \frac{27}{7} < \frac{28}{7}$$

Hence, six rational numbers between $3 = \frac{21}{7}$ and $4 = \frac{28}{7}$ are

$$\frac{22}{7}, \frac{23}{7}, \frac{24}{7}, \frac{25}{7}, \frac{26}{7} \text{ and } \frac{27}{7}$$

Q3. Find five rational numbers between $3/5$ and $4/5$.

Answer:

Since we want 5 rational numbers between $\frac{3}{5}$ and $\frac{4}{5}$, so we write

$$\frac{3}{5} = \frac{3 \times 6}{5 \times 6} = \frac{18}{30}$$

$$\text{and } \frac{4}{5} = \frac{4 \times 6}{5 \times 6} = \frac{24}{30}$$

We know that $18 < 19 < 20 < 21 < 22 < 23 < 24$

$$\Rightarrow \frac{18}{30} < \frac{19}{30} < \frac{20}{30} < \frac{21}{30} < \frac{22}{30} < \frac{23}{30} < \frac{24}{30}$$

Hence, 5 rational numbers between $\frac{3}{5} = \frac{18}{30}$ and $\frac{4}{5} = \frac{24}{30}$

$$\text{are : } \frac{19}{30}, \frac{20}{30}, \frac{21}{30}, \frac{22}{30} \text{ and } \frac{23}{30}$$

Since, we need to find five rational numbers, therefore, multiply numerator and denominator by 6.



Q4. State whether the following statements are true or false. Give reasons for your answers.

(i) Every natural number is a whole number - *True*

∴ The collection of all natural numbers and 0 is called whole numbers.

(ii) Every integer is a whole number - *False*

∴ Negative integers are not whole numbers.

(iii) Every rational number is a whole number - *False*

∴ Rational numbers are of the form p/q , $q \neq 0$ and q does not divide p completely that are not whole numbers.

Exercise 1.2 Page: 8

Q1. State whether the following statements are true or false. Justify your answers.

(i) Every irrational number is a real number – *True*

Because all rational numbers and all irrational numbers form the group (collection) of real numbers.

(ii) Every point on the number line is of the form \sqrt{m} , where m is a natural number – *False*

Because negative numbers cannot be the square root of any natural number.

(iii) Every real number is an irrational number - *False*

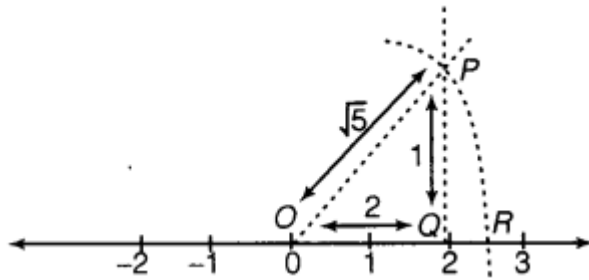
Because rational numbers are also a part of real numbers.

Q2. Are the square roots of all positive integers irrational? If not, give an example of the square root of a number that is a rational number.

Answer: No, if we take a positive integer, say 9, its square root is 3, which is a rational number.

Q3. Show how $\sqrt{5}$ can be represented on the number line.

Answer:



Draw of right angled triangle OQP, such that

OQ = 2 units

PQ = 1 unit

and $\angle OQP = 90^\circ$

Now, by using Pythagoras theorem, we have

$$OP^2 = OQ^2 + PQ^2$$

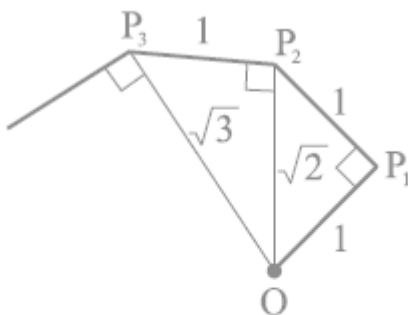
$$= 2^2 + 1^2$$

$$\rightarrow OP = \sqrt{4 + 1} = \sqrt{5}$$

Now, take O as centre OP = $\sqrt{5}$ as radius, draw an arc, which intersects the line at point R.

Hence, the point R represents $\sqrt{5}$.

4. Classroom activity (Constructing the 'square root spiral') : Take a large sheet of paper and construct the 'square root spiral' in the following fashion. Start with a point O and draw a line segment OP_1 of unit length. Draw a line segment P_1P_2 perpendicular to OP_1 of unit length (see Fig. 1.9). Now draw a line segment P_2P_3 perpendicular to OP_2 . Then draw a line segment P_3P_4 perpendicular to OP_3 . Continuing in Fig. 1.9 :



**Fig. 1.9 : Constructing
square root spiral**

Constructing this manner, you can get the line segment $P_{n-1}P_n$ by square root spiral drawing a line segment of unit length perpendicular to OP_{n-1} . In this manner, you will have created the points $P_2, P_3, \dots, P_n, \dots$, and joined them to create a beautiful spiral depicting $\sqrt{2}, \sqrt{3}, \sqrt{4}, \dots$

Solution:



Answer (ii) $\frac{1}{11}$

$$\begin{array}{r} 0.090909 \\ 11 \overline{) 100} \\ \underline{99} \\ 100 \\ \underline{99} \\ 100 \\ \underline{99} \\ 1 \end{array}$$

$\therefore \frac{1}{11} = 0.090909... = 0.\overline{09}$, non-terminating and repeating.

Answer (iii) $4\frac{1}{8}$

$$4\frac{1}{8} = \frac{4 \times 8 + 1}{8} = \frac{33}{8}$$

By long division, we have

$$\begin{array}{r} 4.125 \\ 8 \overline{) 33.000} \\ \underline{32} \\ 10 \\ \underline{8} \\ 20 \\ \underline{16} \\ 40 \\ \underline{40} \\ 0 \end{array}$$

$\therefore \frac{33}{8} = 4.125$, terminating.

Answer (iii) $\frac{3}{13}$

By long division, we have

$$\begin{array}{r} 0.23076923... \\ 13 \overline{) 30} \\ \underline{26} \\ 40 \\ \underline{39} \\ 100 \\ \underline{91} \\ 90 \\ \underline{78} \\ 120 \\ \underline{117} \\ 30 \\ \underline{26} \\ 40 \\ \underline{39} \\ 1 \end{array}$$

Here, the repeating block of digits is 230769

$$\therefore \frac{3}{13} = 0.23076923 = \underline{0.230769}$$

Thus, the decimal expansion of $\frac{3}{13}$ is non-terminating repeating.



Answer (iv): $\frac{2}{11}$

By long division, we have

$$\begin{array}{r} 0.181818... \\ 11 \overline{) 20} \\ \underline{11} \\ 90 \\ \underline{88} \\ 20 \\ \underline{11} \\ 90 \\ \underline{88} \\ 20 \\ \underline{11} \\ 90 \\ \underline{88} \\ 2 \end{array}$$

Here, the repeating block of digits is 18.

$$\therefore \frac{2}{11} = 0.1818... = 0.\overline{18}, =$$

Thus, the decimal expansion of $\frac{2}{11}$ is non-terminating repeating.

Answer (v): $\frac{329}{400}$

By long division, we have

$$\begin{array}{r} 0.8225 \\ 400 \overline{) 3290} \\ \underline{3200} \\ 900 \\ \underline{800} \\ 1000 \\ \underline{800} \\ 2000 \\ \underline{2000} \\ 0 \end{array}$$

$$\therefore \frac{329}{400} = 0.8225, \text{ terminating.}$$



Q2. You know that $\frac{1}{7} = 0.142857$. Can you predict what the decimal expansions of $\frac{2}{7}$, $\frac{3}{7}$, $\frac{4}{7}$, $\frac{5}{7}$, $\frac{6}{7}$ are, without actually doing the long division? If so, how?

[Hint: Study the remainders while finding the value of $\frac{1}{7}$ carefully.]

Answer:

We have, $\frac{1}{7} = 0.\overline{142857}$

$$\therefore \frac{2}{7} = 2 \times \frac{1}{7} = 2 \times 0.\overline{142857}$$

$$\Rightarrow \frac{2}{7} = 0.\overline{285714} ; \frac{3}{7} = 3 \times \frac{1}{7} = 3 \times 0.\overline{142857}$$

$$\Rightarrow \frac{3}{7} = 0.\overline{428571} ; \frac{4}{7} = 4 \times \frac{1}{7} = 4 \times 0.\overline{142857}$$

$$\Rightarrow \frac{4}{7} = 0.\overline{571428} ; \frac{5}{7} = 5 \times \frac{1}{7} = 5 \times 0.\overline{142857}$$

$$\Rightarrow \frac{5}{7} = 0.\overline{714285} ; \frac{6}{7} = 6 \times \frac{1}{7} = 6 \times 0.\overline{142857}$$

$$\Rightarrow \frac{6}{7} = 0.\overline{857142}$$

Thus, without actually doing the long division we can predict the decimal expansions of the given rational numbers.

Q3. Express the following in the form $\frac{p}{q}$ where p and q are integers and $q \neq 0$.

1. $0.\overline{6}$

2. $0.4\overline{7}$

3. $0.\overline{001}$

Answer (i) $0.\overline{6}$

$$0.\overline{6} = 0.666\ldots$$

Assume that $x = 0.666\ldots$

$$\text{Then, } 10x = 6.666\ldots$$

$$10x = 6 + x$$

$$9x = 6$$

$$x = \frac{2}{3}$$



Answer (ii) $0.\overline{47}$

$$\text{Let } x = 0.\overline{47} = 0.4777... \dots (1)$$

As there is only one repeating digit, multiplying (1) by 10 on both sides, we get

$$10x = 4.777$$

Subtracting (1) from (2), we get

$$10x - x = 4.777..... - 0.4777.....$$

$$\Rightarrow 9x = 4.3 \Rightarrow x = \frac{43}{90}$$

Thus, $0.\overline{47} = \frac{43}{90}$

(iii) $0.\overline{001}$

$$0.\overline{001} = 0.001001...$$

Assume that $x = 0.001001...$

Then, $1000x = 1.001001...$

$$1000x = 1 + x$$

$$999x = 1$$

$$x = \frac{1}{999}$$

$$\text{Thus, } 0.\overline{001} = \frac{1}{999}$$

Q4. Express 0.99999.... in the form p/q . Are you surprised by your answer? With your teacher and classmates discuss why the answer makes sense.

Answer:

$$\text{Let } x = 0.99999..... \dots (i)$$

As there is only one repeating digit,

multiplying (i) by 10 on both sides, we get

$$10x = 9.9999 \dots (ii)$$

Subtracting (i) from (ii), we get



$$10x - x = (99999) - (0.9999)$$

$$\Rightarrow 9x = 9 \Rightarrow x = 99 = 1$$

Thus, $0.9999 = 1$

As $0.9999...$ goes on forever, there is no such a big difference between 1 and 0.9999

Hence, both are equal.

Q5. What can the maximum number of digits be in the repeating block of digits in the decimal expansion of $\frac{1}{17}$? Perform the division to check your answer.

Answer: $\frac{1}{17}$

In $\frac{1}{17}$, In the divisor is 17.

Since, the number of entries in the repeating block of digits is less than the divisor, then the maximum number of digits in the repeating block is 16.

Dividing 1 by 17, we have

The remainder 1 is the same digit from which we started the division.

$$\therefore \frac{1}{17} = 0.\overline{0588235294117647}$$

Thus, there are 16 digits in the repeating block in the decimal expansion of $\frac{1}{17}$. Hence, our answer is verified.

$$\begin{array}{r}
 0.0588235294117647... \\
 17 \overline{) 1.0000000000000000} \\
 \underline{-85} \\
 150 \\
 \underline{-136} \\
 140 \\
 \underline{-136} \\
 40 \\
 \underline{-34} \\
 60 \\
 \underline{-51} \\
 90 \\
 \underline{-85} \\
 50 \\
 \underline{-34} \\
 160 \\
 \underline{-153} \\
 70 \\
 \underline{-68} \\
 20 \\
 \underline{-17} \\
 30 \\
 \underline{-17} \\
 130 \\
 \underline{-119} \\
 110 \\
 \underline{-102} \\
 80 \\
 \underline{-68} \\
 120 \\
 \underline{-119} \\
 1
 \end{array}$$



Q6. Look at several examples of rational numbers in the form $\frac{p}{q}$ ($q \neq 0$), where p and q are integers with no common factors other than 1 and having terminating decimal representations (expansions). Can you guess what property q must satisfy?

Answer:

Let us look decimal expansion of the following terminating rational numbers:

$$\frac{3}{2} = \frac{3 \times 5}{2 \times 5} = \frac{15}{10} = 1.5 \quad [\text{Denominator} = 2 = 2^1]$$

$$\frac{1}{5} = \frac{1 \times 2}{5 \times 2} = \frac{2}{10} = 0.2 \quad [\text{Denominator} = 5 = 5^1]$$

$$\frac{7}{8} = \frac{7 \times 125}{8 \times 125} = \frac{875}{1000} = 0.875$$
$$[\text{Denominator} = 8 = 2^3]$$

$$\frac{8}{125} = \frac{8 \times 8}{125 \times 8} = \frac{64}{1000} = 0.064$$
$$[\text{Denominator} = 125 = 5^3]$$

$$\frac{13}{20} = \frac{13 \times 5}{20 \times 5} = \frac{65}{100} = 0.65$$
$$[\text{Denominator} = 20 = 2^2 \times 5^1]$$

$$\frac{17}{16} = \frac{17 \times 625}{16 \times 625} = \frac{10625}{10000} = 1.0625$$
$$[\text{Denominator} = 16 = 2^4]$$

We observe that the prime factorisation of q (i.e. denominator) has only powers of 2 or powers of 5 or powers of both.

Q7. Write three numbers whose decimal expansions are non-terminating non-recurring.

Answer:

$$\sqrt{2} = 1.414213562 \dots\dots\dots$$

$$\sqrt{3} = 1.732050808 \dots\dots\dots$$

$$\sqrt{5} = 2.23606797 \dots\dots\dots$$



Q8. Find three different irrational numbers between the rational numbers 57 and 911 .

Answer:

To find irrational numbers, firstly we shall divide 5 by 7 and 9 by 11,

So,

$$\begin{array}{r} 0.714285... \\ 7 \overline{) 50} \\ \underline{49} \\ 10 \\ \underline{7} \\ 30 \\ \underline{28} \\ 20 \\ \underline{14} \\ 60 \\ \underline{56} \\ 40 \\ \underline{35} \\ 5 \end{array}$$

$$\begin{array}{r} 0.8181... \\ 11 \overline{) 90} \\ \underline{88} \\ 20 \\ \underline{11} \\ 90 \\ \underline{88} \\ 20 \\ \underline{11} \\ 9 \end{array}$$

Thus, $\frac{5}{7} = 0.714285... = 0.\overline{714285}$

$\therefore \frac{5}{7} = 0.\overline{714285}$ and $\frac{9}{11} = 0.\overline{81}$

Three irrational numbers between $0.\overline{714285}$ and $0.\overline{81}$ are

(i) 0.750750075000

(ii) 0.767076700767000

(iii) 0.78080078008000

Q9. Classify the following numbers as rational or irrational:

(1) $\sqrt{23}$

(2) $\sqrt{225}$

(3) 0.3796

(4) 478478...

(5) 1.101001000100001...

Answer:

(1) $\sqrt{23}$ is an irrational number as 23 is not a perfect square.

(2) $\sqrt{225} = \sqrt{3 \times 3 \times 5 \times 5}$; $\therefore 225$ is a perfect square.



3	225
3	75
5	25
5	5
	1

Thus, 225 is a rational number.

(iii) \because 0.3796 is a terminating decimal.

\therefore It is a rational number.

(iv) $7.478478... = 7.\overline{478}$

Since, $7.\overline{478}$ is a non-terminating recurring (repeating) decimal.

\therefore It is a rational number.

(v) Since, 1.101001000100001... is a non-terminating, non-repeating decimal number.

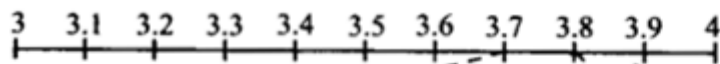
\therefore It is an irrational number.

Exercise 1.4 Page: 18

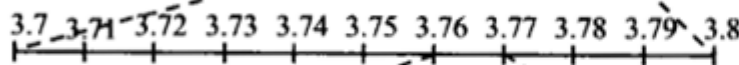
Q1. Visualise 3.765 on the number line, using successive magnification.

Answer:

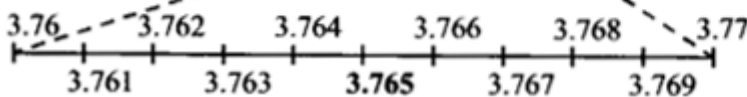
3.765 lies between 3 and 4.



(i) 3.7 lies between 3 and 4



(ii) 3.76 lies between 3.7 and 3.8



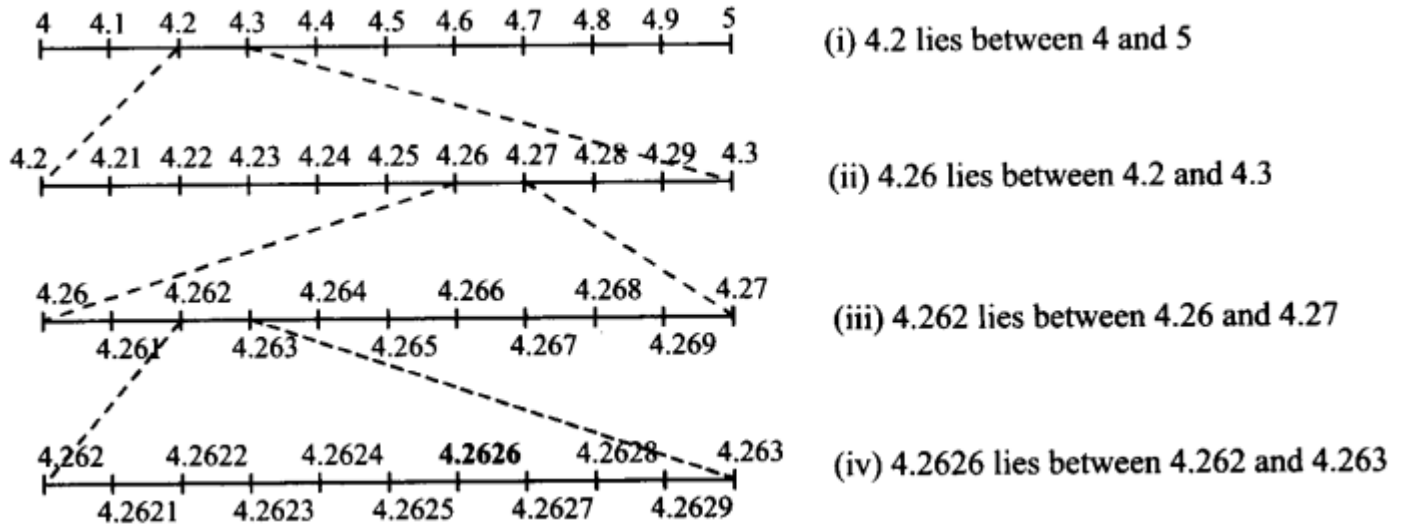
(iii) 3.765 lies between 3.76 and 3.77



Q2. Visualise on $4.\overline{26}$ the number line, up to 4 decimal places.

Answer:

Or $4.\overline{26}$ 4.2626 lies between 4 and 5.



Exercise 1.5 Page: 24

Q1. Classify the following numbers as rational or irrational:

(i) $2 - \sqrt{5}$

Answer:

We know that, $\sqrt{5} = 2.2360679...$

Here, $2.2360679...$ is non-terminating and non-recurring.

Now, substituting the value of $\sqrt{5}$ in $2 - \sqrt{5}$, we get,

$$2 - \sqrt{5} = 2 - 2.2360679... = -0.2360679$$

Since the number, $-0.2360679...$, is non-terminating non-recurring, $2 - \sqrt{5}$ is an irrational number.

(ii) $(3 + \sqrt{23}) - \sqrt{23}$

Answer:

$$(3 + \sqrt{23}) - \sqrt{23} = 3 + \sqrt{23} - \sqrt{23}$$

$$= 3$$

$$= \frac{3}{1}$$



Since the number $3/1$ is in p/q form, $(3 + \sqrt{23}) - \sqrt{23}$ is rational.

(iii) $2\sqrt{7/7}\sqrt{7}$

Solution:

$$2\sqrt{7/7}\sqrt{7} = (2/7) \times (\sqrt{7}/\sqrt{7})$$

We know that $(\sqrt{7}/\sqrt{7}) = 1$

$$\text{Hence, } (2/7) \times (\sqrt{7}/\sqrt{7}) = (2/7) \times 1 = 2/7$$

Since the number, $2/7$ is in p/q form, $2\sqrt{7/7}\sqrt{7}$ is rational.

(iv) $1/\sqrt{2}$

Answer:

Multiplying and dividing numerator and denominator by $\sqrt{2}$ we get,

$$(1/\sqrt{2}) \times (\sqrt{2}/\sqrt{2}) = \sqrt{2}/2 \text{ (since } \sqrt{2} \times \sqrt{2} = 2 \text{)}$$

We know that, $\sqrt{2} = 1.4142...$

$$\text{Then, } \sqrt{2}/2 = 1.4142/2 = 0.7071..$$

Since the number , $0.7071..$ is non-terminating non-recurring, $1/\sqrt{2}$ is an irrational number.

Q2. Simplify each of the following expressions:

(i) $(3 + \sqrt{3}) (2 + \sqrt{2})$

(ii) $(3 + \sqrt{3}) (3 - \sqrt{3})$

(iii) $(\sqrt{5} + \sqrt{2})^2$

(iv) $(\sqrt{5} - \sqrt{2}) (\sqrt{5} + \sqrt{2})$

Answer:

$$\begin{aligned} \text{(i)} \quad (3 + \sqrt{3}) (2 + \sqrt{2}) &= 3(2 + \sqrt{2}) + \sqrt{3}(2 + \sqrt{2}) \\ &= 6 + 3\sqrt{2} + 2\sqrt{3} + \sqrt{6} \end{aligned}$$

$$\begin{aligned} \text{(ii)} \quad (3 + \sqrt{3}) (3 - \sqrt{3}) &= (3)^2 - (\sqrt{3})^2 \quad [\because (a + b) (a - b) = a^2 - b^2] \\ &= 9 - 3 = 6 \end{aligned}$$

$$\begin{aligned} \text{(iii)} \quad (\sqrt{5} + \sqrt{2})^2 &= (\sqrt{5})^2 + 2 \times \sqrt{5} \times \sqrt{2} + (\sqrt{2})^2 \\ &= 5 + 2\sqrt{10} + 2 \quad [\because (a + b)^2 = a^2 + 2ab + b^2] \\ &= 7 + 2\sqrt{10} \end{aligned}$$

$$\begin{aligned} \text{(iv)} \quad (\sqrt{5} - \sqrt{2}) (\sqrt{5} + \sqrt{2}) &= (\sqrt{5})^2 - (\sqrt{2})^2 = 5 - 2 = 3 \\ & \quad [\because (a - b) (a + b) = a^2 - b^2] \end{aligned}$$



Q3. Recall, π is defined as the ratio of the circumference (say c) of a circle to its diameter, (say d). That is, $\pi = c/d$. This seems to contradict the fact that π is irrational. How will you resolve this contradiction?

Answer:

When we measure the length of a line with a scale or with any other device, we only get an approximate fractional value, i.e. c and d both are irrational.

$\therefore \frac{c}{d}$ is irrational and hence π is irrational. Thus, there is no contradiction in saying that it is irrational.

Q4. Represent $(\sqrt{9.3})$ on the number line.

Answer:

Step 1: Draw a 9.3 units long line segment, AB. Extend AB to C such that BC=1 unit.

Step 2: Now, AC = 10.3 units. Let the centre of AC be O.

Step 3: Draw a semi-circle of radius OC with centre O.

Step 4: Draw a BD perpendicular to AC at point B intersecting the semicircle at D. Join OD.

Step 5: OBD, obtained, is a right angled triangle.

Here, OD $\frac{10.3}{2}$ (radius of semi-circle), OC = $\frac{10.3}{2}$, BC = 1

OB = OC – BC

$$\Rightarrow \left(\frac{10.3}{2}\right) - 1 = \frac{8.3}{2}$$

Using Pythagoras theorem,

We get,

$$OD^2 = BD^2 + OB^2$$

$$\Rightarrow \left(\frac{10.3}{2}\right)^2 = BD^2 + \left(\frac{8.3}{2}\right)^2$$

$$\Rightarrow BD^2 = \left(\frac{10.3}{2}\right)^2 - \left(\frac{8.3}{2}\right)^2$$

$$\Rightarrow (BD)^2 = \left(\frac{10.3}{2}\right) - \left(\frac{8.3}{2}\right) \left(\frac{10.3}{2}\right) + \left(\frac{8.3}{2}\right)$$



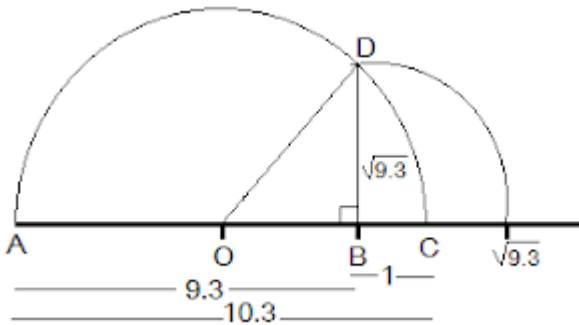
$$\Rightarrow BD^2 = 9.3$$

$$\Rightarrow BD = \sqrt{9.3}$$

Thus, the length of BD is $\sqrt{9.3}$.

Step 6: Taking BD as radius and B as centre draw an arc which touches the line segment.

The point where it touches the line segment is at a distance of $\sqrt{9.3}$ from O as shown in the figure.



Alternative solution:

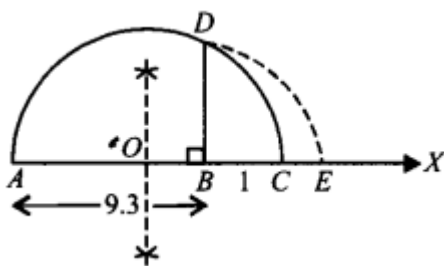
Draw a line segment AB = 9.3 units and extend it to C such that BC = 1 unit.

Find midpoint of AC and mark it as O.

Draw a semicircle taking O as centre and AO as radius. Draw $BD \perp AC$.

Draw an arc taking B as centre and BD as radius meeting AC produced at E such that

$BE = BD = 9.3$ units.





Q5. Rationalise the denominator of the following:

$$(i) \frac{1}{\sqrt{7}} \quad (ii) \frac{1}{\sqrt{7} - \sqrt{6}} \quad (iii) \frac{1}{\sqrt{5} + \sqrt{2}} \quad (iv) \frac{1}{\sqrt{7} - 2}$$

Answer:

$$(i) \frac{1}{\sqrt{7}} \times \frac{\sqrt{7}}{\sqrt{7}} = \frac{\sqrt{7}}{7} \quad (\text{Multiplying and dividing by } \sqrt{7})$$

$$(ii) \frac{1}{\sqrt{7} - \sqrt{6}} \times \frac{\sqrt{7} + \sqrt{6}}{\sqrt{7} + \sqrt{6}} \Rightarrow \frac{\sqrt{7} + \sqrt{6}}{(\sqrt{7})^2 - (\sqrt{6})^2} = \frac{\sqrt{7} + \sqrt{6}}{7 - 6} = \sqrt{7} + \sqrt{6}$$

(Multiplying and dividing by $\sqrt{7} + \sqrt{6}$)

$$(iii) \frac{1}{\sqrt{5} + \sqrt{2}} \times \frac{\sqrt{5} - \sqrt{2}}{\sqrt{5} - \sqrt{2}} = \frac{\sqrt{5} - \sqrt{2}}{(\sqrt{5})^2 - (\sqrt{2})^2} = \frac{\sqrt{5} - \sqrt{2}}{5 - 2} = \frac{\sqrt{5} - \sqrt{2}}{3}$$

(Multiplying and dividing by $\sqrt{5} - \sqrt{2}$)

$$(iv) \frac{1}{\sqrt{7} - 2} \times \frac{\sqrt{7} + 2}{\sqrt{7} + 2} = \frac{\sqrt{7} + 2}{(\sqrt{7})^2 - 2^2}$$

(Multiplying and dividing by $\sqrt{7} + 2$)

$$= \frac{\sqrt{7} + 2}{7 - 4} = \frac{\sqrt{7} + 2}{3}$$

Exercise 1.6 Page: 26

1. Find:

- (i) $64^{1/2}$
- (ii) $32^{1/5}$
- (iii) $125^{1/3}$

Answer:

$$(i) 64^{1/2} = (8 \times 8)^{1/2} = 8^{2 \times \frac{1}{2}} = 8 \quad [\because (a^m)^n = a^{mn}]$$

$$(ii) 32^{1/5} = (2 \times 2 \times 2 \times 2 \times 2)^{1/5} = 2^{5 \times \frac{1}{5}} = 2$$

$$(iii) 125^{1/3} = (5 \times 5 \times 5)^{1/3} = 5^{3 \times \frac{1}{3}} = 5$$



Q2. Find :

(i) $9^{\frac{3}{2}}$

(ii) $32^{\frac{2}{5}}$

(iii) $16^{\frac{3}{4}}$

(iv) $125^{-\frac{1}{3}}$

Answer:

(i) $9^{\frac{3}{2}} = (3^2)^{\frac{3}{2}} = 3^3 = 27$

(ii) $32^{\frac{2}{5}} = (2^5)^{\frac{2}{5}} = 2^2 = 4$

(ii) $16^{\frac{3}{4}} = (2^4)^{\frac{3}{4}} = 2^3 = 8$

(iv) $125^{-\frac{1}{3}} = (5^3)^{-\frac{1}{3}} = 5^{-1} = \frac{1}{5}$

Q3. Simplify:

(i) $2^{\frac{2}{3}} \cdot 2^{\frac{1}{5}}$

(ii) $\left(\frac{1}{3^3}\right)^7$

(iii) $\frac{11^{1/2}}{11^{1/4}}$

(iv) $7^{\frac{1}{2}} \cdot 8^{\frac{1}{2}}$

Answer:

(i) $2^{\frac{2}{3}} \cdot 2^{\frac{1}{5}} = 2^{\frac{2}{3} + \frac{1}{5}} = 2^{\frac{10+3}{15}} = 2^{\frac{13}{15}}$

$(\because x^a \cdot x^b = x^{a+b})$

(ii) $\left(\frac{1}{3^3}\right)^7 = \frac{1}{3^{3 \times 7}} = \frac{1}{3^{21}} = 3^{-21}$

$[\because (x^a)^b = x^{ab}]$

(iii) $\frac{11^{\frac{1}{2}}}{11^{\frac{1}{4}}} = 11^{\frac{1}{2}} \times 11^{-\frac{1}{4}} = 11^{\frac{1}{2} - \frac{1}{4}} = 11^{\frac{2-1}{4}} = 11^{\frac{1}{4}}$

$\left(\because \frac{x^a}{x^b} = x^{a-b}\right)$

(iv) $7^{\frac{1}{2}} \cdot 8^{\frac{1}{2}} = (7 \cdot 8)^{\frac{1}{2}} = (56)^{\frac{1}{2}}$

$[\because x^a \cdot y^a = (xy)^a]$